# MODELS FOR MANAGING INCOMPLETE INFORMATION IN RECOMMENDER SYSTEMS

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#### ABSTRACT

Recommender Systems have recently emerged to assist network users in their search processes, due to the fact, these users must deal with a vast quantity of information that is stored in huge data bases of different e-shops, e-libraries, etc. The Recommender Systems help them in their search by means of recommendations that arise from information provided by different sources as the proper user, experts, other users, etc. Most of the current Recommender Systems force their users to provide the information in an only way, usually a numerical scale. Nevertheless, the information provided by the different sources get to use incomplete, vague and imprecise because it is related to their own perceptions, tastes and preferences. In other research areas as decision analysis, planning, scheduling, etc., this type of information has been successfully managed allowing the sources of information to express their preferences by means of different representation models and preference structures. In this contribution we shall review these models and structures together several resolution processes dealing with them in order to propose their use in the Recommender Systems to improve their accuracy and success in the recommendations.

#### KEYWORDS

Recommender systems, preference modeling, uncertainty, accuracy,

## **1. INTRODUCTION**

One of the main problems users face navigating in Internet is the vast quantity of information they find. It is such amount of information that companies such as google (www.google.com) or amazon (www.amazon.com) use Recommender Systems to assist users in their search. The Recommender Systems are a class of software (P. Resnick and H.R.Varian, 1997) that has emerged in the last years within the domain of the E-Commerce (J.B. Schafer et al., 2001). Traditionally, these systems have fallen in three main categories: (i) *Collaborative filtering systems* (ii) *Content-based filtering systems* and (iii) *Hybrid content-based and collaborative recommender systems*.

These systems gather preference information from users, experts, etc., related to their preferences, tastes, and opinions about a given type of items (books, music, etc). Such a way that using this information the system ranks the items, and makes a recommendation about what items are the most attractive for each user. These systems can be seen as a kind of decision making process that tries to obtain a solution set of alternative/s (recommendations) from the information provided by the sources of information. And this information get to use subjective, vague and incomplete because it is related to the own perceptions of the sources. In spite of this, the most common way that the Recommendation Systems require the information to their sources is by means of a precise numerical scale (C. Hayes and P. Cunningham, 2001). This obligation implies a lack of expressiveness and hence a lack of precision in the recommendations. In the decision analysis literature we can find different ways to express this type of information by means of different representation models and preference structures together their respective resolution schemes have provided successful results (F. Chiclana et al., 1998; F. Herrera et al., 2004, Q. Zhang et al., K. Jae Kyeong and C. Sang Hyun, 2001). The application of these tools to Recommendation Systems can improve the effectiveness of the recommendations given by the Recommender Systems if they are able to deal with different representation models and preference structures according to the nature and uncertainty of the features and aspects assessed by the sources of information. Here, we shall review different representation models, preference structures and resolution models that have been used in the literature to deal with incomplete, vague and uncertain information in order to propose that Recommendation Systems can handle and offer these tools to support their users in their searching process improving their recommendations.

This contribution is set out as follows: Section 2 we present a general view of Recommender Systems. Section 3 we show different representation models and preference structures used to deal with vague and imprecise information. In the section 4, we review different resolution methods dealing with the above models and structures and finally we shall outline our future work in recommender systems.

# 2. A GENERAL VIEW OF RECOMMENDER SYSTEMS

Recommender Systems are a class of software to assist people in their search process in Internet or other networking processes. Their purpose is to recommend the most suitable items, from a set of items according to the customer, user's desires. This recommendation is made using different preferences and opinions gathered by the Recommender Systems from different types of sources. Most of Recommender Systems use one or two types of information sources. However, there exist at least five different types of information sources that can be used to obtain better recommendations (A. Ansari et al., 2000):

- 1. A person's expressing preferences or choices among alternative products.
- 2. Preferences for product attributes.
- 3. Other people's preferences or choices.
- 4. Expert Judgments.
- 5. Individual characteristics that may predict preferences.

A good recommendation system should be able to use any or all of these five types of information, potentially making better recommendations as more information become available.

Current recommender systems fall into three classes depending on the type of information and sources they use to make recommendations:

- 1. *Collaborative filtering systems* (D. Goldberg et al., 1992): they use explicit and implicit preferences from many users to filter and recommend objects to a given user, ignoring the representation of the objects. In the simplest case, these systems predict a person's preference as a weighted sum of other people's preferences, in which the weights are proportional to correlations over a common set of items evaluated by two people. Collaborative filtering algorithms were first introduced by Golberg and colleagues (D. Goldberg et al., 1992). They are used by Los Angeles Times, London Times, CRAYON, and Tango to customize online newspaper; by Movie Critic, Moviefinder and Morse to recommend movies; by barnesandnoble.com to recommend books, etc.
- 2. *Content-based filtering systems:* filter and recommend the items by matching user query terms with the index term used in the representation of the items, ignoring data from other users (M. Pazzani et al., 1996). There are some commercial systems has been offered by PersonalLogic, Frictionless Commerce, and Active Research that use self-explicated importance ratings and/or attribute trade-offs to make their recommendations.
- 3. *Hybrid content-based and collaborative recommender systems*: This new class has emerged between the content-based and collaborative recommender systems and its aim is to smooth out the disadvantages of each one of them. A usual way to hybrid both classes is to make a two level filter algorithm, where we use first one of the algorithm (the content-based filtering algorithm) to obtain the first set of items and afterwards, we use the second algorithm (the collaborative filtering algorithm) to filter and recommend items from this set (C. Basu et al., 1998).

So far, we have seen what type of information is used by the Recommender Systems and we have aforementioned that most of the Recommender Systems force their sources to provide their information using a numerical scale despite, this information is vague, imprecise and uncertain. Our aim is to propose that these systems manage this information as in other areas in the literature such as Decision Making (Q. Zhang et al.); System for management support for restoring aquatic ecosystems and drainage areas (A. Jimenez et al., 2003), Information Systems evaluation problem (K. Jae Kyeong and C. Sang Hyun, 2001.) in order to improve the effectiveness of their recommendations.

## 3. INFORMATION REPRESENTATION MODELS AND STRUCTURES

In this section, we show different information representation models and preference structures that have been used in the literature to express and handle incomplete and vague information, where the information structures are referred to how the information is organized and the representation model is referred to the nature and domain in which the information is assessed by the source of information.

### **3.1 Information representation models**

When we deal with incomplete, vague and imprecise information, the aspects assessed could have different nature (quantitative or qualitative) or the knowledge that the sources have on the aspects could be different as well. So according to the nature of the aspects qualified and the knowledge that the sources have on them this information could be expressed in different ways:

#### A) QUANTITATIVE ASPECTS

- Numerical values: if they are easy measurable the sources of information assess them by means of precise numerical values, so, we could work with a value scale, where the maximum value is the best rating and minimum value is the worst rating. However, when the items are related to qualitative aspects or when the knowledge about the items presents uncertainty it may be difficult to qualify them using precise values.
- □ Interval values: sometimes uncertainty is quite difficult to assess using a crisp and precise number although the aspect is quantitative. The first approach used in the literature to add some flexibility to the uncertainty representation problem was the use of intervals. In this case, the sources are not able to give a numerical value of a quantitative attribute but can provide their preference information using interval values assessed in a range (J.F. Le Téno and B. Mareschal, 1998).

#### **B) QUALITATIVE ASPECTS**

□ Linguistic values: these aspects are realted to human perception. To model them, a better approach may be to use linguistic assessments instead of numerical values. The fuzzy linguistic approach represents qualitative aspects as linguistic values by means of linguistic variables (L.A. Zadeh, 1975).

When we deal with linguistic information, we have to choose the appropriate linguistic descriptors for the term set and their semantics. In order to accomplish this objective, an important aspect to analyze is the "granularity of uncertainty", i.e., the level of discrimination among different counts of uncertainty. The universe of the discourse over which the term set is defined can be arbitrary, usually linguistic term sets are defined in the interval [0, 1].

One possibility of generating the linguistic term set consists of directly supplying the term set by considering all terms distributed on a scale on which a total order is defined (R.R. Yager, 1995). For example, a set of seven terms S, could be given as follows:

 $S = \{s_0 = \text{None}; s_1 = \text{Very Low}; s_2 = \text{Low}; s_3 = \text{Medium}; s_4 = \text{High}; s_5 = \text{Very High}; s_6 = \text{Perfect}\}$ 

in these cases, it is usually required that there exist:

- (a) A negation operator  $Neg(s_i) = s_j$  such that j = g i (g+1 is the cardinality).
- (b) A minimization and a maximization operator in the linguistic term set.

The semantics of the terms is given by fuzzy numbers defined in the [0,1] interval, which are described by membership functions. A way to characterize a fuzzy number is to use a representation based on parameters of its membership function (Bonissone and Decker (1986)). For example, we may use triangular membership functions and assign the following semantics to the set of seven terms, S, which is graphically shown in Figure 1.



Figure 1: A set of seven terms and their semantics

# **3.2 Information Structures**

When the sources of information provide their preferences so important is the representation model as the way to organize the information. Here we are going to show the different ways the sources can organize their information over a set of items  $X = \{x_1, \ldots, x_n\}$  using different information structures:

- 1. Preference ordering of the items: In this case, the source,  $s_k$ , provides his preferences on X as an individual preference ordering,  $O^k = \{o^k(1), ..., o^k(n)\}$ , where  $o^k(\cdot)$  is a permutation function over the index set,  $\{1, ..., n\}$  (F. Chiclana et al., 2001). Therefore, according to this viewpoint, an ordered vector of items, from the best one to the worst one, is given:  $O^k = \{i_1, i_2, i_3, i_5, i_4\}$ .
- 2. A preference relation: With this representation, a source's preference,  $s_k$ , on X is describe by a preference matrix  $A^k \subset X \times X$ ,  $A^k = [a_{ij}^k]$ , where  $a_{ij}^k$  indicates the preference intensity for item  $x_i$  to that of  $x_j$  (T. Tanino, 1984), i.e.  $R: X \times X \to A$ . The value,  $R(x_i, x_j) = p_{ij}$ , denotes the degree to which an item  $x_i$  is preferred to an item  $x_i$  where  $p_{ii} \in A$ :

$$P_{e_k} = \begin{pmatrix} p_{11} & \cdots & p_{1n} \\ \vdots & \cdots & \vdots \\ p_{n1} & \cdots & p_{nn} \end{pmatrix}$$

Where A can be any of the information representation models that has been seen in the section 3.1. 3. An utility vector: In this case, the source,  $s_k$ , provides its preferences on X as a set of n utility values,  $U^k = \{u_i^k, i = 1, ...n\}, u_i^k \in A$ , where  $u_i^k$  represents the utility evaluation given by the source  $s_k$  to the item  $x_i$  (T. Tanino, 1990), i.e.:  $U^k = \{u_1^k, u_2^k, u_3^k, u_4^k\}$  is the evaluation of the set of items  $I = \{i_1, i_2, i_3, i_4\}$ . Where  $u_i^k \in A$  and A can be any of the information representation models that has been seen in the section 3.1.  $u_i^k$  represents the evaluation given to the item  $i_i$  and the most preferred item is the item that has the greatest evaluation, the worst item is the item that has the lowest evaluation.

## 4. DEALING WITH INCOMPLETE INFORMATION.

In the before section we have shown how can be represented and organised the vague and uncertain information by the sources of information. Due to the similarity between the processes carry out by the Recommendation Systems and the Decision Making processes in this section we shall review different literature about decision processes dealing with incomplete information modelled wit different representation models and preference structures (See Table 1).

INFORMATION CONTEXT	MODEL
- Numerical and interval values.	P. Kyung Sam et al., 1996; K. Soung Hie et al., 1999;
- Preference ordering of the items and utility vector.	K. Jae Kyeong et al., 1998; K. Jae Kyeong and C.
	Sang Hyun, 2001;
	K. Soung Hie and A. Byeong Seok, 1997; K. Soung
	Hie and A. Byeong Seok, 1999
- Numerical and interval values.	Zhang et al.
- Preference relations, preference ordering of the	
items, utility vector.	
<ul> <li>Linguistic values, numerical values.</li> </ul>	F. Herrera and L. Martinez. 2001, F. Chiclana et al.,
- Preference ordering of the items, preference	1998
relations, utility vector.	
<ul> <li>Linguistic values, numerical values.</li> </ul>	M. Delgado et al., 1998
- Preference relations.	
- Linguistic values, numerical values.	F. Herrera and L. Martinez, 1999
- Utility vector.	
- Multi-granularity linguistic values.	F. Herrera et al., 2000;F. Herrera and L. Martinez.
- Utility vector.	2001;F. Herrera and L. Martinez, 2001 (b)

Table 1. Decision Resolution Methods Dealing With Incomplete Information.

# 5. FUTURE WORKS

In the future we want to use several of the methods presented in the Table 1 in the Recommendation Systems processes to improve the results of these systems. We shall mainly focus on the methods and models presented in (F. Chiclana et al., 1998; F. Herrera et al., 2004) such that the Recommendation Systems can deal with:

1. Numerical information.

4. Preference ordering vectors.

2. Interval information.

5. Preference relations.

3. Linguistic information.

6. Utility vectors.

Several of these methods and models have been used successfully in Decision Making and evaluation processes in (L. Martínez et al, 2004) and in (L.G. Pérez et al., 2004) we can find a first approach, in recommender systems, of a model that try to manage this kind of problems.

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